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KEY STAGE

**ALL TIERS** 

Mathematics tests

Mark scheme

for Paper 2

Tiers 3-5, 4-6, 5-7 and 6-8





National curriculum assessments

## Introduction

This booklet contains the mark scheme for paper 2 at all tiers. The paper 1 mark scheme is printed in a separate booklet. Questions have been given names so that each one has a unique identifier irrespective of tier.

#### The structure of the mark schemes

The marking information for each question is set out in the form of tables, which start on page 10 of this booklet. The columns on the left-hand side of each table provide a quick reference to the tier, question number, question part and the total number of marks available for that question part.

The 'Correct response' column usually includes two types of information:

- a statement of the requirements for the award of each mark, with an indication of whether credit can be given for correct working, and whether the marks are independent or cumulative
- examples of some different types of correct response, including the most common.

The 'Additional guidance' column indicates alternative acceptable responses, and provides details of specific types of response that are unacceptable. Other guidance, such as when 'follow-through' is allowed, is provided as necessary.

Questions with a *Using and applying mathematics (UAM)* element are identified in the mark scheme by the symbol (u1). The number indicates the significance of using and applying mathematics in answering the question. The U number can be any whole number from 1 to the number of marks in the question.

For graphical and diagrammatic responses, including those in which judgements on accuracy are required, marking overlays have been provided as the centre pages of this booklet.

The 2009 key stage 3 mathematics tests and mark schemes were developed by the Test Development Team at Pearson Research and Assessment.

# General guidance

### Using the mark schemes

Answers that are numerically equivalent or algebraically equivalent are acceptable unless the mark scheme states otherwise.

In order to ensure consistency of marking, the most frequent procedural queries are listed on the following two pages with the prescribed correct action. This is followed by further guidance relating specifically to the marking of questions that involve money, negative numbers, time, measures, coordinates, probability or algebra. Unless otherwise specified in the mark scheme, markers should apply the following guidelines in all cases.

### Recording marks awarded on the test paper

All questions, even those not attempted by the pupil, should be marked, with a 1 or a 0 entered in each marking space. Where 2m can be split into 1m gained and 1m lost, with no explicit order, then this will be recorded by the marker as 1m

The total marks awarded for a double page should be written in the box at the bottom of the right-hand page, and the total number of marks obtained on the paper should be recorded on the front of the test paper.

A total of 120 marks is available in each of tiers 3–5, 4–6, 5–7 and 6–8.

### **Awarding levels**

The sum of the marks gained on paper 1, paper 2 and the mental mathematics paper determines the level awarded. Level threshold tables, which show the mark ranges for the award of different levels, will be available on the NAA website www.naa.org.uk/tests from April 2009.

What if	Marking procedure		
The pupil's response is numerically or algebraically equivalent to the answer in the mark scheme.	Markers should award the mark unless the mark scheme states otherwise.		
The pupil's response does not match closely any of the examples given.	Markers should use their judgement in deciding whether the response corresponds with the statement of the requirements given in the 'Correct response' column. Refer also to the 'Additional guidance'.		
The pupil has responded in a non-standard way.	Calculations, formulae and written responses do not have to be set out in any particular format. Pupils may provide evidence in any form as long as its meaning can be understood. Diagrams, symbols or words are acceptable for explanations or for indicating a response. Any correct method of setting out working, however idiosyncratic, should be accepted. Provided there is no ambiguity, condone the continental practice of using a comma for a decimal point.		
There appears to be a misreading affecting the working.	This is when the pupil misreads the information given in the question and uses different information without altering the original intention or difficulty level of the question. For each misread that occurs, deduct one mark only.		
No answer is given in the expected place, but the correct answer is given elsewhere.	but the given. In particular, where a word or number response is expected, a pupil mais given meet the requirement by annotating a graph or labelling a diagram elsewhere		
The final answer is wrong, but the correct answer is shown in the working.	Where appropriate, detailed guidance will be given in the mark scheme and must be adhered to. If no guidance is given, markers will need to examine each case to decide whether:		
	the incorrect answer is due to a transcription error	If so, award the mark.	
	<ul> <li>in questions not testing accuracy, the correct answer has been given but then rounded or truncated</li> </ul>	If so, award the mark.	
	<ul> <li>the pupil has continued to give redundant extra working which does not contradict work already done</li> </ul>	If so, award the mark.	
	<ul> <li>the pupil has continued, in the same part of the question, to give redundant extra working which does contradict work already done.</li> <li>If so, do not award the mark. Where a question part carries more than one mark, only the final mark should be withheld.</li> </ul>		
The pupil's answer is correct but the wrong working is shown.	A correct response should always be marked as correct unle states otherwise.	ess the mark scheme	

What if	Marking procedure		
The pupil has made a conceptual error.	In some questions, a method mark is available provided the pupil has made a computational, rather than conceptual, error. A computational error is a 'slip' such as writing $4 \times 6 = 18$ in an otherwise correct long multiplication. A conceptual error is a more serious misunderstanding of the relevant mathematics; when such an error is seen, no method marks may be awarded. Examples of conceptual errors are:		
	• misunderstanding of place value, such as multiplying by 2 rather than 20 when calculating $35 \times 27$		
	• subtracting the smaller value from the larger in calculations such as 45 – 26 to give the answer 21		
	incorrect signs when working with negative numbers.		
The correct response has been crossed or rubbed out and not replaced.	Any legible crossed or rubbed out work that has not been replaced should be marked according to the mark scheme. If the work is replaced, then crossed or rubbed out work should not be considered.		
More than one answer is given.	If all answers given are correct (or a range of answers is given, all of which are correct), the mark should be awarded unless prohibited by the mark scheme. If both correct and incorrect responses are given, no mark should be awarded.		
The pupil's answer correctly follows through from earlier incorrect work.	Follow-through marks may be awarded only when specifically stated in the mark scheme, but should not be allowed if the difficulty level of the question has been lowered. Either the correct response or an acceptable follow-through response should be marked as correct.		
The answer is correct but, in a later part of the question, the pupil has contradicted this response.	A mark given for one part should not be disallowed for working or answers given in a different part, unless the mark scheme specifically states otherwise.		
The pupil's accuracy is marginal according to the overlay provided.	Overlays can never be 100% accurate. However, provided the answer is within or touches the boundaries given, the mark(s) should be awarded.		
The pupil has drawn lines which do not meet at the correct point.	Markers should interpret the phrase 'lines not accurate' to mean meeting within or on a circle of radius 2mm with centre at the correct point.  Within the circle accepted on the circle accepted outside the circle not accepted		

# Responses involving money

	✓ Accept	× Do not accept
Where the £ sign is given for example: £3.20, £7	<ul> <li>✓ f3.20</li> <li>f7</li> <li>f7.00</li> <li>Any unambiguous indication of the correct amount, eg</li> <li>f3.20p</li> <li>f3 20 pence</li> <li>f3 20</li> <li>f3,20</li> <li>f3,20</li> <li>f3:20</li> <li>320p with £ sign crossed out</li> </ul>	Incorrect placement of pounds or pence, eg f320 f320p Incorrect placement of decimal point, or incorrect use or omission of 0, eg f3.2 f3 200 f32 0 f3-2-0
Where the p sign is given for example: 40p	<ul> <li>✓ 40p         Any unambiguous indication of the correct amount, eg         £0.40p         £.40p         £0.40 with p sign crossed out     </li> </ul>	Incorrect or ambiguous use of pounds or pence, eg 0.40p £40p
Where no sign is given for example: £3.20, 40p	<ul> <li>✓ f3.20</li> <li>320p</li> <li>40p</li> <li>f0.40</li> <li>Any unambiguous indication of the correct amount in £ or p as shown above</li> <li>At levels 3 and 4 only also accept omission of units, eg</li> <li>3.20</li> <li>320</li> <li>40</li> <li>0.40</li> </ul>	Mark Omission of final zero, eg 3.2 0.4

# Responses involving negative numbers

	✓ Accept	×	Do not accept
For example: -2			To avoid penalising the error below more than once within each question, do not award the mark for the first occurence of the error within each question. Where a question part carries more than one mark, only the final mark should be withheld.
		×	Incorrect notation, eg 2-

### Responses involving time

	✓ Accept	x Do not accept
A time interval for example: 2 hours 30 minutes	✓ 2 hours 30 minutes  Any unambiguous, correct indication, eg 2 ½ hours 2.5 hours 2h 30 2h 30 min 2 30  Digital electronic time, ie 2:30	Incorrect or ambiguous time interval, eg 2.3 hours 2.3h 2h 3 2.30 min 2.30 2-30 2,30 2.30
A specific time for example: 8:40am, 17:20	<ul> <li>✓ 8:40am</li> <li>8:40</li> <li>twenty to nine</li> <li>Any unambiguous, correct indication, eg</li> <li>08.40</li> <li>8.40</li> <li>0840</li> <li>8 40</li> <li>8-40</li> <li>8,40</li> <li>Unambiguous change to 12 or 24 hour clock, eg</li> <li>17:20 as 5:20pm or 17:20pm</li> </ul>	Incorrect time, eg 8.4am 8.40pm Incorrect placement of separators, spaces, etc or incorrect use or omission of 0, eg 840 8:4:0 8.4 084 84

### Responses involving measures

	✓ Accept	× Do not accept
Where units are given (eg kg, m, l) for example: 8.6kg	<ul> <li>✓ 8.6kg         Any unambiguous indication of the correct measurement, eg         8.60kg         8.6000kg         8kg 600g     </li> </ul>	➤ Incorrect or ambiguous use of units, eg 8600kg

#### Note

If a pupil leaves the answer box empty but writes the answer elsewhere on the page, then that answer must be consistent with the units given in the answer box and the conditions listed above.

If a pupil changes the unit given in the answer box, then their answer must be equivalent to the correct answer, using the unit they have chosen, unless otherwise indicated in the mark scheme.

### Responses involving coordinates

For example:

(5, 7)

#### ✓ Accept

✓ Unconventional notation, eg

(05, 07) (five, seven)

*x y* (5, 7)

(x=5, y=7)

#### x Do not accept

 $oldsymbol{x}$  Incorrect or ambiguous notation, eg

(7, 5)

y x (7, 5)

(5x, 7y)

 $(5^x, 7^y)$ 

(x-5, y-7)

### Responses involving probability

A numerical probability

should be expressed as

a decimal, fraction or

percentage only.

for example:

#### ✓ Accept

✓ Equivalent decimals, fractions and percentages, eg

2.700

0.700

70 100

35 50

70.0%

! Take care 🗴 Do not accept

The first **four** categories of error below should be ignored if accompanied by an acceptable response, but should not be accepted on their own.

However, to avoid penalising the first **three** types of error below more than once within each question, do not award the mark for the *first* occurrence of each type of error unaccompanied by an acceptable response. Where a question part carries more than one mark, only the final mark should be withheld.

✓ A probability correctly expressed in one acceptable form which is then incorrectly converted, but is still less

than 1 and greater than 0, eg

 $\frac{70}{100} = \frac{18}{25}$ 

! A probability that is incorrectly expressed, eg

7 in 10

7 over 10

7 out of 10

7 from 10

! A probability expressed as a percentage without a percentage sign.

! A fraction with other than integers in the numerator and/or denominator.

! A probability expressed as a ratio, eg 7:10

7:3

7 to 10

➤ A probability greater than 1 or less than 0

#### 8

## Responses involving the use of algebra

Responses involving the use of algebra						
	✓ Accept	! Take care × Do not accept				
For example: 2 + n n + 2 2n \frac{n}{2} n^2	✓ Unambiguous use of a different case or variable, eg N used for n x used for n	! Unconventional notation, eg $n \times 2$ , or $2 \times n$ , or $n2$ or $n + n$ for $2n$ $n \times n$ for $n^2$ $n \div 2$ for $\frac{n}{2}$ or $\frac{1}{2}n$ $2 + 1n$ for $2 + n$ $2 + 0n$ for $2$ Within a question that demands simplification, do not accept as part of a final answer involving algebra. Accept within a method when awarding partial credit, or within an explanation or general working.				
	✓ Words used to precede or follow equations or expressions, eg	<ul> <li>Embedded values given when solving equations, eg</li> <li>in solving 3x + 2 = 32, 3 × 10 + 2 = 32 for x = 10</li> <li>To avoid penalising the two types of error below more than once within each question, do not award the mark for the first occurrence of each type within each question. Where a question part carries more than one mark, only the final mark should be withheld.</li> <li>! Words or units used within equations or expressions, eg</li> </ul>				
	t = n + 2 tiles or tiles $= t = n + 2for t = n + 2Unambiguous letters used to indicate expressions, eg t = n + 2 for n + 2$	<ul> <li>n tiles + 2</li> <li>n cm + 2</li> <li>Do not accept on their own. Ignore if accompanying an acceptable response.</li> <li>* Ambiguous letters used to indicate expressions, eg</li> <li>n = n + 2 for n + 2</li> </ul>				

		& Questi -6 5–7				School shop
1			Mark	Correct response	Additional guidance	
а	1		1m	19		
b	)		1m	Friday	✓ Unambiguous indication eg, for part (b)	
C			1m (U1)	Ruler	<ul><li>F</li><li>eg, for part (c)</li><li>R</li></ul>	

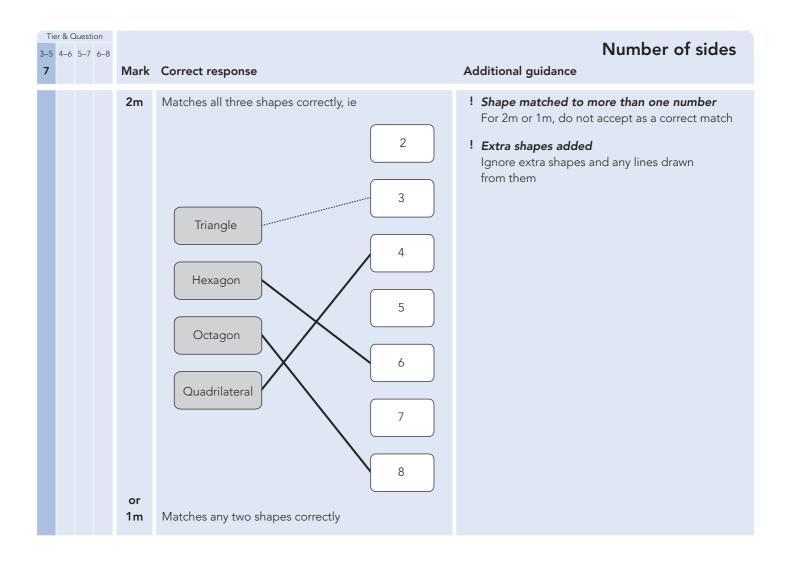
	Questi 5–7	on 6–8				Missing numbers
2			Mark	Correct response	Additional guidance	J
			1m	26		
			1m	3		

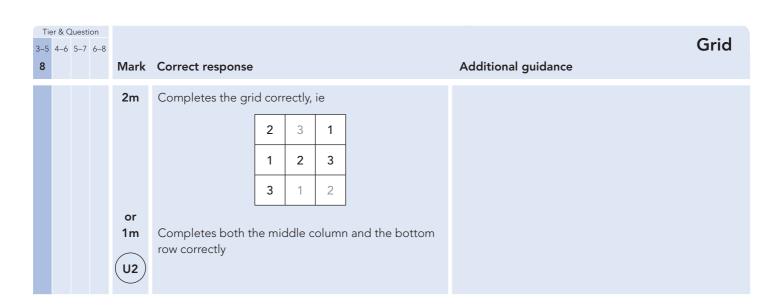
Tier & Question  3–5 4–6 5–7 6–8  3 Ma	rk Correct response	Parcels Additional guidance
2n oi 1n	•	

Tier & Question  3–5 4–6 5–7 6–8  Mai	ark Correct response	Joining Additional guidance
or 1m	eg  Draws any two of the three different sized squares	<ul> <li>! Lines not ruled or accurate</li></ul>

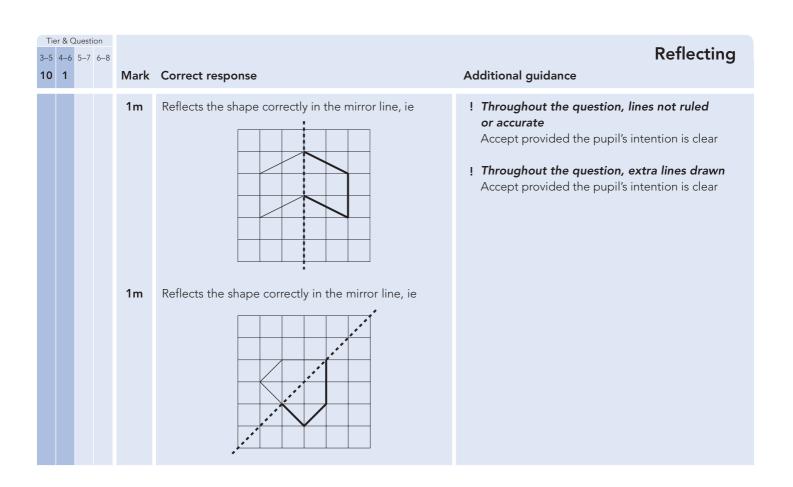
Tier & Question  3–5 4–6 5–7 6–8 <b>5</b> Mark	Correct response	Additional guidance	Spinner
2m or 1m	Makes all four correct decisions, ie  True False  V	<ul> <li>✓ Unambiguous indication</li> <li>eg</li> <li>✓ for True, ★ for False</li> </ul>	

	er & Question 4–6 5–7 6–8	Mark	Correct response	Fractions Additional guidance
а		1m	Indicates any three squares	<ul> <li>! Squares not shaded         Accept any unambiguous indication</li> <li>! Part squares indicated         Accept provided the pupil's intention is clear</li> </ul>
b		1m	$\frac{3}{5}$ or equivalent	<b>≭</b> Equivalent decimals





	Question 5-7 6-	3		Digital
9		Mark	Correct response	Additional guidance
		1m	10:45	<ul> <li>! Indication of am or pm</li> <li>Condone either am or pm shown or implied eg, accept</li> <li>10:45 am</li> <li>22:45</li> </ul>
		1m	Gives a correct description of the time in words eg  • Five past ten	<ul> <li>Words and numbers used in description         Condone, provided the time has been interpreted correctly eg, accept         5 past 10     </li> </ul>
				<ul><li>'Digital time' described in words</li><li>eg</li><li>Ten O five</li></ul>
				<ul> <li>Description of time incorrect or using numbers eg</li> <li>Ten five</li> <li>10 5</li> </ul>



		Question 5–7			Test	
12	2		Mark	Correct response	Additional guidance	
а	а		1m	С		
b	b		1m	21		
			U1)			

	ier & C	Rounding			
13	3		Mark	Correct response	Additional guidance
а	а		1m	2700	
			1m	3000	
b	b		1m	Gives a value greater than or equal to 795 but less than 805	√ 800

4–6	Questi 5–7	Mark	Correct response	Castle Additional guidance
		2m	f 5(.00)	
		or 1m	Shows the value 22(.00)  or  Shows or implies a complete correct method with not more than one computational error eg  • 12.00 (error) + 9 = 21.00 Answer given as 4.00	

	er & Q 4–6				Baby
14	5		Mark	Correct response	Additional guidance
а	а		1m	4	<b>★</b> Any reference to extra days
b	b		1m	9	× Any reference to extra weeks or days

	er & C					Count on
15	6		Mark	Correct response	Additional guidance	
а	а		1m	27		
b	b		2m	1		
			or 1m	Shows or implies that the size of two steps is 4 eg  • 4 4 7  • -3 + 4  or  Shows or implies that the size of one step is 2 eg  • The gaps are 2  • -3 + 2  • Second number is -1  • Fourth number is 3  • -3 to 5 is 8, 8 ÷ 4	★ Shows steps of unequal size	

3–5	er & C 4–6 <b>7</b>		Mark	Correct response	Shoe sizes Additional guidance
а	а		1m	12	
b	b		1m	3	
С	c		1m	Indicates Both the same and gives a correct explanation  The most common correct explanations:  Use given values eg  Range of boys is 4, range of girls is 4  8 – 4 is the same as 9 – 5  5 to 9 = 4 to 8	<ul> <li>✓ Minimally acceptable explanation eg</li> <li>• 4, 4</li> <li>• 8 - 4, 9 - 5</li> <li>• Both 4</li> <li>! Ambiguous notation eg</li> <li>• 4 - 8, 5 - 9</li> <li>Condone</li> </ul>
			(U1)	Reason generally about spread eg • Boys cover 5 sizes, girls cover 5 sizes	<ul> <li>✓ Minimally acceptable explanation eg         <ul> <li>Both have the same number of sizes</li> </ul> </li> <li>! Explanation implies references to the number of blank sizes         <ul> <li>eg</li> <li>Boys have one blank, girls have one blank</li> <li>Because the girls didn't have size 9 and the boys didn't have size 4             <ul> <li>Condone</li> </ul> </li> <li>★ Ambiguous or incorrect explanation eg</li> <li>5 in each</li> <li>They both have a range of five sizes</li> <li>Girls: 4, 5, 6, 7, 8                   <ul> <li>Boys: 5, 6, 7, 8, 9</li> </ul> <li>Boys: 5, 6, 7, 8, 9</li> </li></ul> <li>Boys: 5,</li></li></ul>

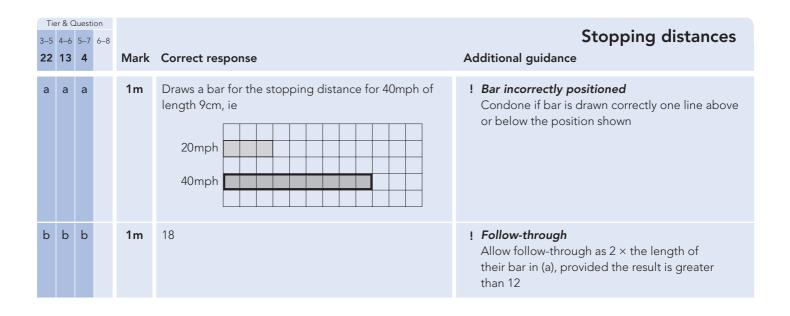
			Questi 5–7				Finding $x$ and $y$
1	7	8		Mark	Correct response	Additional guidance	
				1m	652		
				1m	442		

Tier & Question 3–5 4–6 5–7 6–i 18 9		Correct response	Seventy Additional guidance
	1m	Indicates No and gives a correct explanation that shows or implies at least one odd factor eg  • Factors of 70 are 1, 2, 5, 7, 10, 14, 35 and 70, so some are odd and some are even  • There are four odd factors and four even factors of 70  • It could be 1 (odd)  • 5 × 14 = 70  • 70 ÷ 2 = 35  • 70 is even, but 1 is odd and goes into everything	<ul> <li>✓ Minimally acceptable explanation         eg             • 1, 2, 5, 7, 10, 14, 35 and 70             • 7              ! Incomplete list of factors given                   Condone, provided none is incorrect and at least one odd factor is shown                   eg, accept                   • The factors of 70 are 1, 2, 5 and 7</li></ul>

	ier & C										Units
20	10	1	Mark	Correct re	esponse					Additional guidance	
			2m	Complete	s all five r	ows of th	e table co	orrectly, ie			
					L	Α	V	М			
				cm	<b>√</b>						
				1			✓				
				miles	✓						
				g				✓			
				m <sup>2</sup>		✓					
				oz				✓			
			<i>or</i> 1m	Complete	es at least	three row	vs of the t	able corre	ectly		

		Questio			Rainforest
3–5 <b>19</b>		5–7	Maula	Command washington	
19	11	2	iviark	Correct response	Additional guidance
а	а	а	1m	27	
b	h	b	1m	175 to 185 inclusive	
D	b	d	ım	1/3 to 163 inclusive	
С	С	С	1m	Indicates January, ie	

Tier & Question  3–5   4–6   5–7   6–8  21   12   3	Mark	Correct response	Doughnuts Additional guidance
	or 1m	Indicates shop A and gives a correct justification, based on correctly calculating a pair of comparable values eg  • At shop A: 2 × 5 = 10, at shop B: 3.5(0) × 3 = 10.5(0)  • 3.5 × 3 - 2 × 5 = 0.5  • 2 ÷ 3 = 0.6(), 3.50 ÷ 5 = 0.7  • For £1 you get \$1\frac{1}{2}\$ doughnuts or \$1\frac{3}{7}\$ doughnuts  • You pay £1.50 extra for 2 more doughnuts, but at shop A they're less than 75p each so shop A must be a better deal  Shows a correct pair of comparable values but makes either an incorrect or no decision or  Shows a complete correct method for finding a pair of comparable values with not more than one computational or rounding error, and follows through to make their correct decision eg  • 5 × 2, 3 × 3.50, shop A indicated  • 2 ÷ 3 = 0.75 (error), 3.50 ÷ 5 = 0.7, shop B indicated  or  Makes a correct decision but the justification uses only the difference between a pair of comparable values eg  • A doughnut is 3.3()p cheaper at shop A	<ul> <li>★ For 2m, no decision</li> <li>✓ For 2m, correct decision and any pair of comparable values shown         Note that common pairs (in pounds) are:         <ul> <li>10 and 10.5(0) (per 15 doughnuts)</li> <li>0.6() and 0.7(0) (per 1 doughnut)</li> <li>2 and 2.1(0) (per 3 doughnuts)</li> <li>3.3() and 3.5(0) (per 5 doughnuts)</li> <li>1.5 and 1.4() (doughnuts per pound)</li> </ul> </li> <li>For 2m or 1m, comparison is per 3 doughnuts or per 5 doughnuts but the given price is not restated         <ul> <li>Condone</li> <li>eg, for 2m accept</li> <li>At shop B, 3 doughnuts would be £2.10</li> </ul> </li> <li>! Additional incorrect working Ignore</li> </ul>

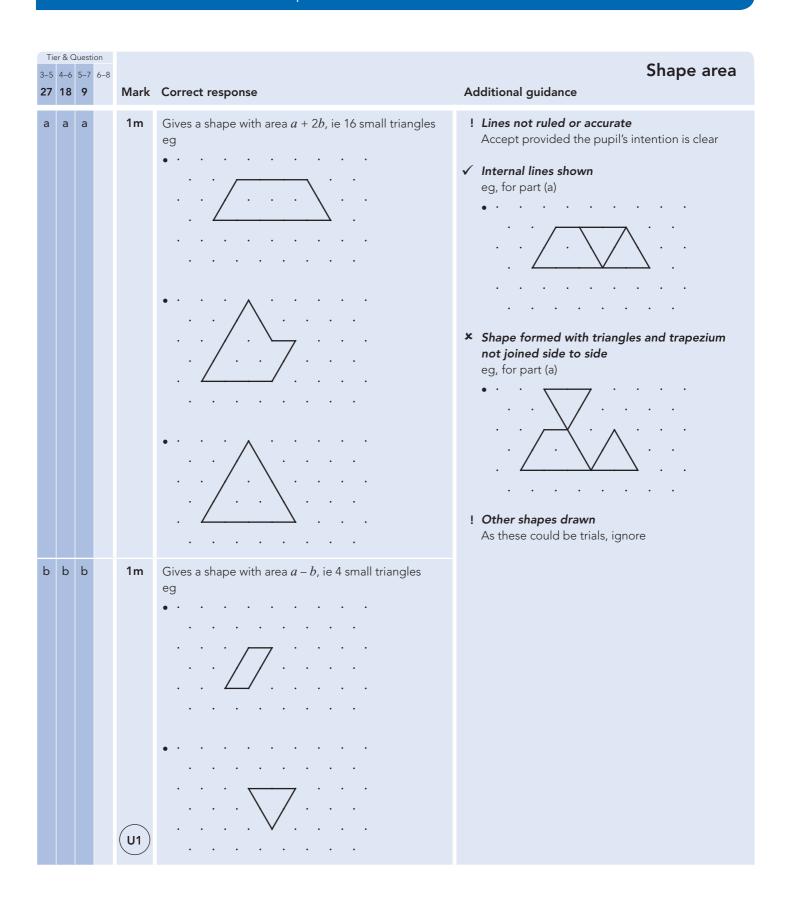


3–5	Suestion 5–7 6–8 <b>5</b>		Marking overlay available  Correct response	Rotate 180 Additional guidance
		2m or 1m	Draws the correct shape with all four vertices within the tolerances as shown on the overlay  Shows at least three vertices within the tolerances as shown on the overlay  or  Shows a correct shape in the correct orientation, with all four vertices within the tolerances as shown on the overlay, but in an incorrect position on the grid	! Lines not ruled or accurate Accept provided the pupil's intention is clear

3–5	4–6	Questi 5 5-7 6 6	6-8	Mark	Correct response	Value Additional guidance
				1m	196	<b>★</b> Incomplete processing
				1m	4	
				1m	1225	

Tier & Question 12 cubes 3–5 4–6 5–7 6–8 25 16 7 Mark Correct response Additional guidance Draws a 1 by 1 by 12, a 1 by 3 by 4 or a 2 by 2 by 3 x 1 by 2 by 6 cuboid repeated 2m cuboid, using the isometric grid √ For 2m or 1m, internal lines omitted eg eg, for 2m accept ! For 2m or 1m, hidden lines shown For 2m, accept provided they are clearly indicated as hidden lines eg, for 2m accept or 1m The only error is to omit some external lines or to ! Lines not ruled show some hidden lines Accept provided the pupil's intention is clear eg ! Drawing not accurate Accept vertices within 2mm of the dots of the grid x Isometric grid not used correctly ! Other shapes drawn As these could be trials, ignore Correctly draws a possible 3-D shape made from 12 cubes that is not a cuboid, using the isometric grid eg

3–5		Σuestion 5–7 6	5–8	Mark	Correct response	Cost of delivery  Additional guidance
а	а	а		1m	Gives both correct values correctly positioned, ie 7 then 20  Gives a correct value with the correct unit for that	<ul> <li>✓ Range given instead of 20</li> <li>eg</li> <li>0 - 20</li> </ul>
				•••	value eg • 25p • 25 pence • £0.25	
b	b	b		1m	18.25	



3–5 4	& Ques -6 5-: 1 <b>9 10</b>	7 6–8	Mark	Correct response	Midpoints Additional guidance
			1m	Gives P as (30, 35)	
			1m	Gives Q as (42, 0)	! Answers for P and Q transposed but otherwise completely correct If this is the only error, ie gives P as (42, 0) and gives Q as (30, 35), mark as 0, 1
			1m (U1)	Gives R as (42, 35)	! Follow-through for R as (their x coordinate of Q, their y coordinate of P) Allow follow-through provided their coordinates for P, Q and R are different

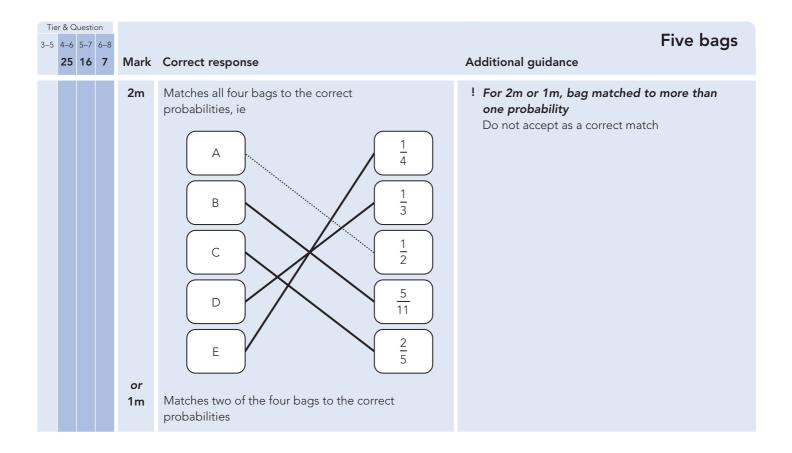
Tier & Question 3–5 4–6 5–7			Rainfall
	Mark	Correct response	Additional guidance
	or 1m	Indicates place A and gives a correct justification eg  • 10 × 8 + 20 × 4 = 160cm  5 × 10 + 50 × 2 = 150cm  • (80 + 80) ÷ 12 = 13.()cm per month  (50 + 100) ÷ 12 = 12.5cm per month  • (80 + 80) ÷ 2 = 80cm per 6 months  (50 + 100) ÷ 2 = 75cm per 6 months  Gives a correct justification, even if the decision is incorrect or omitted  or  Shows a complete correct method with not more than one computational error, and follows through to make their correct decision eg  • 10 × 8 + 20 × 4 = 120 (error)  5 × 10 + 50 × 2 = 150, so place B	<ul> <li>✓ For 2m, minimally acceptable justification eg</li> <li>160, 150 seen</li> <li>80, 80 and 50, 100 seen</li> <li>10 × 8 + 20 × 4 &gt; 5 × 10 + 50 × 2</li> <li>13.(), 12.5 seen</li> </ul>

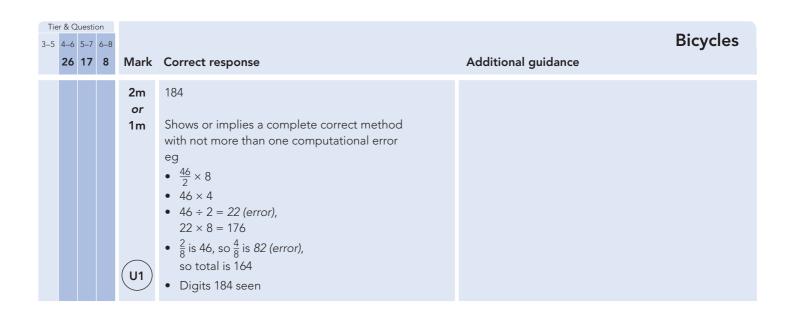
	Questi 5–7				Thinking distances
21	12	3	Mark	Correct response	Additional guidance
а	a	a	2m or 1m	315 Shows the value 245 or	
				Shows a complete correct method, in which the 'squared' has been correctly interpreted, with not more than one computational error eg  • $70 + \frac{70 \times 70}{20}$ • $70^2 = 4900$ , $4900 \div 20 = 2450$ (error), $70 + 2450 = 2520$	
b	b	b	1m	50	

Tier & Question 3–5 4–6 5–7 6–8				Two shapes
22 13 4	Mark	Correct response	Additional guidance	
	2m	60		
	or 1m	Shows the value 6 or Shows a complete correct method with not more than one computational error eg  • $72 \div 12 = 8 \text{ (error)}$ , $10 \times 8 = 80$		

Tier & Question 3–5 4–6 5–7 6–8 23 14 5 Mark	Correct response	Additional guidance	Recycling
2m or 1m	760 000  Shows the value 1 240 000  or  Shows a complete correct method with not more than one error eg  • 2 000 000 × 0.38  • 38 ÷ 100 × 2 × 1 000 000  • 2 million = 20 000 000 (error) 20 000 000 × 0.38 = 7 600 000		

Tier & 3–5 4– <b>2</b> 4		6–8	Mark	Correct response	Shapes on a grid Additional guidance
а	а	а	1m	Gives a correct explanation  The most common correct explanations:  Refer to the sum of the angles in a triangle eg  • The angles are equal and add up to 180, so 180 ÷ 3 = 60  • Angles in a triangle add up to 180, the three	<ul> <li>✓ Minimally acceptable explanation eg</li> <li>180 ÷ 3</li> <li>60 × 3 = 180</li> <li>The angles are the same and add up</li> </ul>
				Refer to the sum of angles at a point eg  • You can see that six of the triangles fit together at a point, so $360 \div 6 = 60$	to 180 <b>x</b> Incomplete explanation eg  • The three angles add up to 180 • Angles in a triangle add up to 180 • The three angles are equal • 60 × 3 • It's an equilateral triangle  ✓ Minimally acceptable explanation eg • 360 ÷ 6 • 60 × 6 = 360 <b>x</b> Incomplete explanation eg • Six of the angles add up to 360 • Angles at a point add up to 360
b	b	b	2m or 1m	Total: 360  Gives all three correct angles, ie $a = 60$ , $b = 120$ and $c = 240$ Gives two correct angles	• $60 \times 6$ ! For 1m, follow-through Provided their $b$ is obtuse, accept $c$ as $2 \times$ their $b$ or $360$ – their $b$





Tier & C	 6–8	Mark	Correct response	Additional guidance	Eggs
		or 1m	Indicates the grade is medium and shows or implies a correct method for calculating the mass of the egg that interprets the 'cubed' correctly, even if a final value is not shown eg  • Value between 60 and 60.12 inclusive seen  • $5.5 \times 5.5 \times 5.5 \times \pi \div 10 \times 1.15$ • $166.375 \times \pi \times 0.115$ Makes an incorrect or no decision about the grade of the egg, but shows or implies a correct method for calculating the mass of the egg that interprets the 'cubed' correctly, even if a final value is not shown eg  • $5.5 \times 5.5 \times 5.5 \times \pi \div 10 \times 1.15$ • $522.7 \div 10 \times 1.15$		
			Shows or implies a correct method for calculating the mass of the egg that interprets the 'cubed' correctly, with not more than one computational or rounding error, and makes their correct decision for the grade of the egg eg  • 5.5 <sup>3</sup> × 3 (error) ÷ 10 × 1.15 = 57.(), so medium  • 5.5 <sup>3</sup> = 166 (premature rounding), 166 × 3.14 × 0.115 = 59.9(), so medium	<ul> <li>For 1m, final value and decision not shown within a method containing a computational or rounding error</li> <li>For 1m, conceptual error eg         <ul> <li>5.5³ = 16.5, 16.5 × π ÷ 10 × 1.15 = 5.9() or 6, so small</li> </ul> </li> </ul>	

Tier & 3–5 4–6					Ring size
			Mark	Correct response	Additional guidance
	а	а	1m	57 or 57.1() or 57.2	
	b	b	or 1m	Indicates size 6 and gives a correct justification eg  • $51 \div \pi = 16.2()$ • $51 \div 3.14 = 16.2()$ • $16.5 \times \pi = 51.8()$ or $52$ • $16.5 \times \pi = 49.()$ • $16.5 \times \pi = 51.8()$ and $15.7 \times \pi < 51$ Shows a correct justification but makes an incorrect or no decision or  Indicates size 6 and gives an incomplete justification eg  • $51 \div \pi$ • $51 \div 3.14$ • $51.8()$ or $52$ • $49.()$	<ul> <li>✓ For 2m, minimally acceptable justification eg</li> <li>16.2()</li> <li>49.() and 51.8() or 52 seen</li> <li>✗ For 2m, incomplete justification eg</li> <li>51 ÷ π</li> <li>51 ÷ 3.14</li> <li>16.5 × π = 51.8()</li> <li>✗ For 1m, incorrect or no justification alongside a correct decision eg</li> <li>51 ÷ 3 = 17, so size 6</li> <li>Because the circumference of a size 6 is 51</li> </ul>

Tier & Question 3-5 4-6 5-7 6-8 20 11	Mark	Correct response	Missing power
	or 1m	Shows correct working and gives the value of $x$ as 3 eg  • $3^5 + 10^2 = 343$ • $7 \times 7 \times 7 = 343$ • $3^5 = 243$ , $10^2 = 100$ $343 \div 7 = 49$ , $49 \div 7 = 7$ • $7^3 = 343$ Gives the value of $x$ as 3, even if working is incomplete or omitted  or  Shows the value $343$ or	<ul> <li>! Value embedded Accept provided there is no ambiguity and correct working is shown eg, for 2m accept <ul> <li>7³ shown in correct working eg, for 2m do not accept</li> <li>7³ on the answer line, even with correct working</li> </ul> </li> </ul>

Tier & Question 3–5 4–6 5–7 6– 21 13	-8	Correct response	School size Additional guidance
	or 1m	Shows that the average number of pupils in a secondary school is about four times as many as the average number in a primary school eg  • Primary school: 4 069 385 ÷ 17 642  = 230.() (or 231)  Secondary school: 3 315 805 ÷ 3385  = 979.() (or 980)  979 ÷ 230 = 4.2()  • 17 642 ÷ 3 385 = 5.2()  4 069 385 ÷ 3 315 805 = 1.2()  5.2() ÷ 1.2() = 4.2() or 4.3 recurring  Shows the values 230.() (or 231) and 979.() (or 980)  or  Shows the intention to divide the total number of pupils by the number of schools for both categories using any reasonably rounded values eg  • 4 069 385 ÷ 17 642, 3 315 805 ÷ 3385  • 4 100 000 ÷ 18 000, 3 300 000 ÷ 3000  • 4 000 000 ÷ 18 000, 3 000 000 ÷ 3000	<ul> <li>✓ For 2m, minimally acceptable justification eg</li> <li>979.() ÷ 230.()</li> <li>980 ÷ 231</li> <li>4 100 000 ÷ 18 000 ÷ (3 300 000 ÷ 3000)</li> <li>980, 4 × 230 = 920</li> <li>231, 980 ÷ 4 = 245</li> </ul>

Tier & Qu 3–5 4–6 5					Container
2	22 13	Mark	Correct response	Additional guidance	
		2m or 1m	Shows or implies a complete correct method with not more than one error eg  12000 ÷ 800  12000 ÷ (40 × 20)  Shows the digits 15		

Tier & Questi 3–5 4–6 5–7 <b>23</b>	6–8	Mark	Correct response			nth term expressions Additional guidance
		3m	Completes all thre	e rows of the tab	ole correctly, ie	✓ Unambiguous indication of 'Yes' or 'No'
			Expression	<i>n</i> th term expression?	4th term	✓ Space for 4th term left blank for the expression n + 11
			5 <i>n</i>	No	×	
			n + 11	No	×	
			11 <i>n</i> – 6	Yes	38	
			$n^2(6-n)$	Yes	32	
		or 2m or 1m	Completes two row correctly or Completes the mide even if the right-harmonic correct correctly or completes the mide even if the right-harmonic correct corre	he row for the e for the expressic	xpression on $n^2(6-n)$ he table correctl	

Tier & Questic 3–5 4–6 5–7 <b>24</b>	6–8	Mark	Correct response	Additional guidance	Exam
		Mark 2m or 1m	Shows or implies a complete correct method eg  • Total mark on 6 units must be 80 × 6 = 480 Total so far = 78 × 5 = 390 480 - 390  • 80 × 6 - 78 × 5  • 80 - 78 = 2, 2 × 5 = 10, 80 + 10  or  Shows the value 480 or 390  or  Shows or implies a complete correct method with not more than one computational error eg  • Total mark on 6 units must be 80 × 6 = 420 (error) 420 - 78 × 5 = 30	Additional guidance  ✓ For 2m, reference to 100 marks eg • 90 out of 100 • 90/100	
			<ul> <li>80 × 6 – 78 × 5</li> <li>80 – 78 = 2, 2 × 5 = 10, 80 + 10</li> </ul>		

Tier & 3–5 4–6	5 5–7	6–8	Mark	Correct response	Additional guidance	Equations
	а	а	1m	Indicates both correct equations, ie		
	Ь	b	1m	Gives two pairs of coordinates for which $y = x + 1$ and gives a correct equation eg  • (3, 4) and (0, 1) $y = x + 1$ • (1, 2) and (2, 3) $x = y - 1$ • (-2, -1) and $\left(\frac{1}{2}, 1\frac{1}{2}\right)$ $y - x = 1$	! Unconventional notation eg, for $y = x + 1$ • $y1 = 1 \times x + 1$ Condone	

er & Q 4–6	5–7	6–8		Correct response	House sales Additional guidance
	а	а	1m	75 000	
	b	b	1m	$33\frac{1}{3}$	! Value rounded Accept 33 or better
		С	1m	64 000	

	Questi				Standard form
		18	Mark	Correct response	Additional guidance
			1m	Indicates $2 \times 10^8$ and $2.5 \times 10^8$ , in either order	<ul> <li>✓ Unambiguous indication</li> <li>eg, for part (a)</li> <li>• 200 000 000 and 250 000 000</li> </ul>

Tier & Qu 3–5 4–6 5				(	Greater
	19		Correct response	Additional guidance	
	а	1m	d, by 7		
	b	1m	<i>f</i> , by 1		

Tier & Question 3-5 4-6 5-7 6-8 20 Mark	Correct response	Three years old
2m or 1m	558 000  Shows the value 557 551.()  or  Shows a complete correct method with not more than one computational or rounding error, even if their value is not rounded to the nearest thousand eg  • 546 400 ÷ 98 × 100  • 550 000 (premature rounding) ÷ 0.98 = 561 224	<ul> <li>✓ 558 thousand</li> <li>★ For 1m, conceptual error</li> <li>eg</li> <li>0.02 × 546 400 + 546 400</li> <li>= 557 328</li> </ul>

Tier & Question  3–5 4–6 5–7 6–8  21	Mark	Correct response	Height Additional guidance
	or 1m	7.2 or 7.18()  Shows or implies a correct trigonometric ratio eg  17 × sin 25 $\frac{h}{17}$ = sin 25  17 × cos 65	<ul> <li>Method used is accurate or scale drawing</li> <li>For 2m, answer of 7         Do not accept unless a correct method or a more accurate value is seen     </li> <li>Units given Ignore</li> </ul>

Tier & Que 3–5 4–6 5	Mark	Correct response	Fewest me	en
	2m or 1m	Shows the digits 114() or 115  or  Shows a complete correct method with not more than one computational or rounding error eg  • 100 ÷ 87 × 100  • 100 ÷ 87 = 1.1 (premature rounding), 1.1 × 100 = 110		

ier & Q 5 4–6	5–7	6–8	Mark	Correct response	Daisies Additional guidance	
		а	1m	32		
		b	1m	7		
		С	1m	25		

Tier & Question 3–5 4–6 5–7 6–8 24 Mark	Correct response	Using Pythagoras  Additional guidance
2m or 1m	Shows or implies a correct method, using Pythagoras' theorem, for calculating the length of the missing side of the right-angled triangle with a hypotenuse of 22cm eg  • $x^2 = 22^2 - 20^2$ • $x = \sqrt{84}$ • $\sqrt{(22^2 - 20^2)}$ • $\sqrt{84}$ • $2\sqrt{21}$ • 9.165	<ul> <li>! Value of 20 or 21  Do not accept unless a correct method or a more accurate value is seen</li> <li>! For 1m, value rounded or truncated  Accept 9.1() or 9.2  Do not accept 9 unless a correct method or a more accurate value is seen</li> </ul>

Tier & Question 3–5 4–6 5–7 6–8 25	Mark	Correct response	Booklet Additional guidance
	3m or 2m	Shows a correct value for the mass of the booklet eg  • 59.8752  or  Shows or implies a correct method with not more than one error or omission, and follows through to give their value correct to 2 significant figures, provided some rounding is required eg  • 297 × 420 × 6 = 748 440, 748 440 × 80 = 59 875 200, so 60 000 000 [failure to convert to m²]  • 297 × 420 ÷ 1000 (error) = 124.74, 124.74 × 6 × 80 = 59 875.2, so 60 000 [incorrect conversion to m²]  • 0.297 × 0.42 × 80 = 10 [failure to find mass of 6 pages]  Shows or implies a correct method with not more than one error or omission, even if their value is not given correct to 2 significant figures eg  • 0.297 × 0.42 × 6 × 80  • 297 × 420 × 6 = 748 440, 748 440 × 80 (error) = 59 875 200  • 0.297 × 0.42 × 80 = 9.9()	! For 2m, value rounded or truncated Accept 59, 59.8() or 59.9

Tier & Question 3-5 4-6 5-7 6-8			Hemisphere
26	Mark	Correct response	Additional guidance
	2m	Completes the table correctly with two fully simplified expressions, ie	
		Radius Volume Surface area	
		$r$ $\frac{2}{3}\pi r^3$ $3\pi r^2$	
	or		_
	1m	Gives one correct and fully simplified expression	on
		or	
		Gives both correct, unsimplified expressions eg	
		Radius Volume Surface area	
		$r$ $\frac{4}{3}\pi r^3 \div 2$ $2\pi r^2 + \pi r^2$	
		•	٦
		Radius Volume Surface area	
		$r$ $\frac{4}{6}\pi r^3$ $3\pi r \times r$	
			_

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